VASAVI COLLEGE OF ENGINEERING (AUTONOMOUS), HYDERABAD M.C.A. (CBCS) III-Semester Main Examinations, December-2018

## Operations Research

Time: 3 hours
Max. Marks: 60
Note: Answer ALL questions in Part-A and any FIVE from Part-B

| Q.No. | Stem of the question |
| :---: | :--- |
| Part- $\boldsymbol{A}(10 \times 2=20$ Marks) |  |
| 1. | What is the canonical form of a LPP? |
| 2. | State the general linear programming problem and define (i) feasible <br> solution and (ii) basic feasible solution. |

3. List any three approaches used with transportation problem, for determining the starting solution.
4. What do you understand by degeneracy in a transportation problem?
5. Give the Linear Programming form of the assignment problem.
6. What is Integer Programming?
7. State the formula for EOQ under manufacturing model where shortages are allowed.
8. What types of Games are solved graphically?
9. What is meant by Minimize and Maximize?
10. Define EOQ.

$$
\text { Part-B }(5 \times 8=40 \text { Marks })
$$

11. a) Solve by simplex method:

Maximize $Z=3 x_{1}+5 x_{2}+4 x_{3}$
Subject to

$$
\begin{aligned}
& 2 x_{1}+3 x_{2} \leq 8 \\
& 2 x_{2}+5 x_{3} \leq 10 \\
& 3 x_{1}+2 x_{2}+4 x_{3} \leq 15 \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{aligned}
$$

b) Solve the LPP
$\operatorname{Max} \mathrm{z}=2 \mathrm{x}_{1}+3 \mathrm{x}_{2}+5 \mathrm{x}_{3}$
Subject to $3 \mathrm{x}_{1}+10 \mathrm{x}_{2}+5 \mathrm{x}_{3} \leq 15$

$$
33 x_{1}-10 x_{2}+9 x_{3} \leq 33
$$

$$
x_{1}+2 x_{2}+x_{3} \geq 4
$$

$$
x_{1}, x_{2}, x_{3} \geq 0
$$

12. a) Explain Transshipment Model - II.
b) Solve the transportation problem

Destinations

Origin

13. a) A company is faced with the problem of assigning 4 machines to 6 different jobs (one machine to one job only). The profits are estimated as follows:

Machine

Job

| Machine |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| A |  |  |  | B |
| 1 | C | D |  |  |
| 2 | 3 | 6 | 2 | 6 |
|  | 7 | 1 | 4 | 4 |
| 4 | 3 | 8 | 5 | 8 |
| 4 | 6 | 4 | 3 | 7 |
|  | 5 | 2 | 4 | 3 |
|  | 5 | 7 | 6 | 4 |

Solve the problem to maximize the total profit by branch and bound technique.
13. b) Find the optimum integer solution of the integer programming problem:

$$
\begin{gathered}
\operatorname{Max} Z=7 x_{1}+9 x_{2} \\
\text { Subject to } \begin{array}{c}
x_{1}+3 x_{2} \leq 6 \\
7 x_{1}+x_{2} \leq 35
\end{array}
\end{gathered}
$$

and $x_{1}, x_{2}$ are non-negative integers
14. a) A commodity is to be supplied at a constant rate of 200 units per day. Supplies for any amounts can be had at any required time, but each ordering costs Rs. 50.00 costs of holding the commodity in inventory is Rs. 2.00 per unit per day while the delay in the supply of the items induces a penalty of Rs. 10.00 per unit per delay of one day. Formulate the average cost function of this situation and find the optimal policy ( $\mathrm{q}, \mathrm{t}$ ) where t is the reorder cycle period and q is the inventory level after re-order. What should be the best policy if the penalty cost becomes infinite?
b) A company has a demand of 12,000 units/year for an item and it can produce 2000 such items per month. The cost of one setup is Rs. 400 and the holding cost/unit/month is Rs. 0.15 . Find the optimum lot size, max inventory, manufacturing time, total time.
15. a) Find the optimum strategies and the value of the game
X

$\mathbf{X}$| 4 | -1 | 4 | -1 | 2 |
| :---: | :---: | :---: | :---: | :---: |
| 2 | 2 | 3 | -4 | 2 |
| 1 | -3 | 1 | 0 | -4 |

b) Solve graphically

| Player A | B |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 2 | 3 |
|  | 1 | 3 | 3 | 4 | 0 |
|  | 2 | 5 | 4 | 3 | 7 |

16. a) Solve the LPP
$\operatorname{Max} \mathrm{z}=2 \mathrm{x}_{1}+\mathrm{x}_{2}$
Subject to $\quad 3 x_{1}+x_{2} \geq 3$
$4 x_{1}+3 x_{2} \geq 6$
$x_{1}+2 x_{2} \geq 2$
and $x_{1}, x_{2} \geq 0$
423

4332

4342
$\begin{array}{llll}4 & 2 & 4 & 2\end{array}$
$\begin{array}{llll}4 & 3 & 5 & 2\end{array}$
$\begin{array}{llll}4 & 2 & 5 & 2\end{array}$
$\begin{array}{llll}4 & 2 & 1 & 2\end{array}$

Contd... 3
b) Find the initial basic feasible solution for the following transportation problem by VAM

17. Answer any two of the following:
a) A department has four subordinates, the subordinates and four tasks are to be performed. The subordinates differ in efficiency and tasks differ in their intrinsic difficulties. The estimate of time (in hours) each man would take to perform each tasks is given by

Tasks

Subordinate

|  | I II III IV |  |  | IV |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 8 | 26 | 17 | 11 |
| 2 | 13 | 28 | 4 | 26 |
| 3 | 38 | 19 | 18 | 15 |
| 4 | 19 | 26 | 24 | 10 |

Find out how the tasks be allotted to man so as to optimize the total manhours.
b) A manufacturing company purchases 9000 parts of a machine for its annual requirements, ordering one month usage at a time. Each part costs Rs. 20. The ordering cost per order is Rs. 15 and the carrying charges are $15 \%$ of the average inventory per year. You have been asked to suggest a more economical purchasing policy for the company. What advice would you offer, and how much would it save the company per year?
c) Solve the following game

$$
\text { Player A }\left[\begin{array}{ccc}
\text { Player B } \\
{\left[\begin{array}{ccc}
-1 & 2 & 1 \\
1 & -2 & 2 \\
3 & 4 & -3
\end{array}\right]}
\end{array}\right.
$$

